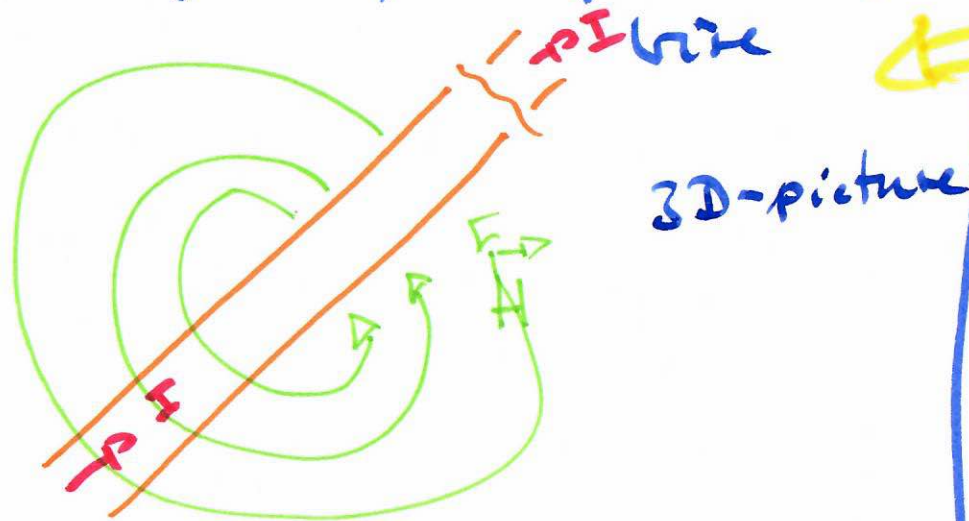


16.12.18 Electric Machinery

Basics of magnetic field

- Each current has a magnetic field AND each magnetic field has a current, also PM (Permanent mag.)
- The magnetic field of a straight



3D-picture

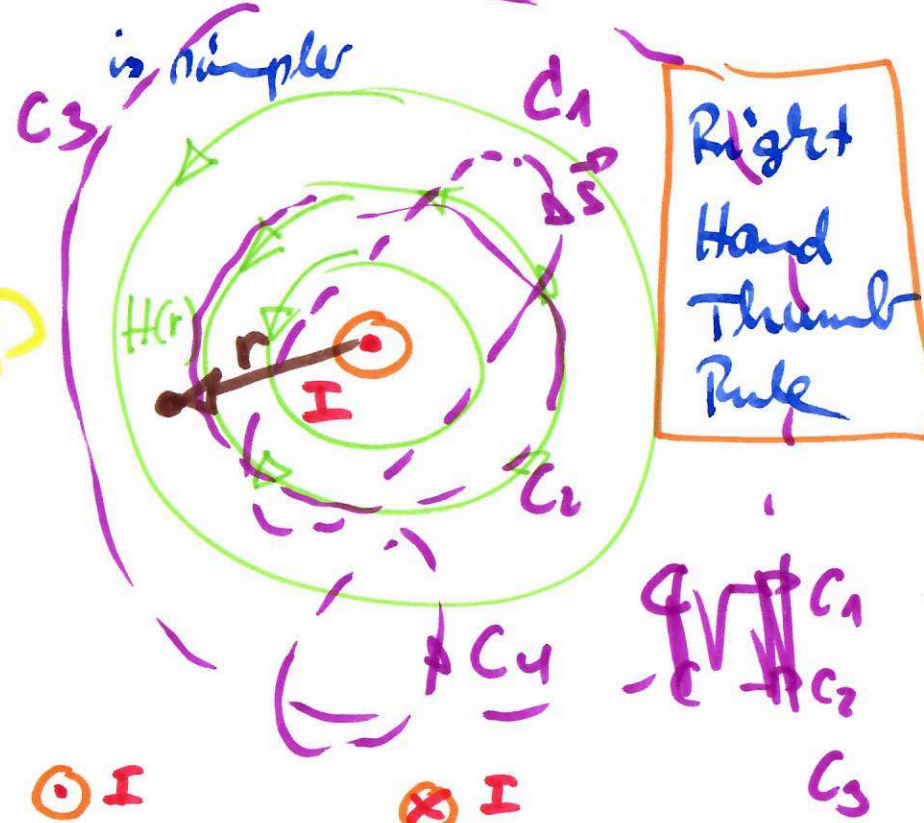
$\vec{H}$: magnetic field strength
 $\vec{H}$ is a vector
 $[H] = A/m$

①

②

$\vec{H} = \vec{H}(x, y, z, t)$: complicated

only in some special cases we can handle it "by hand".
in this case a 2D-picture is simpler



Right Hand Thumb Rule

$\odot I$

Current goes to the top

$\otimes I$

current goes into the paper

C_3

$$H(r) = \frac{I}{2\pi r}$$

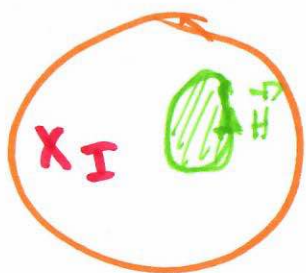
• From where does it come?

The law of Biot-Savart

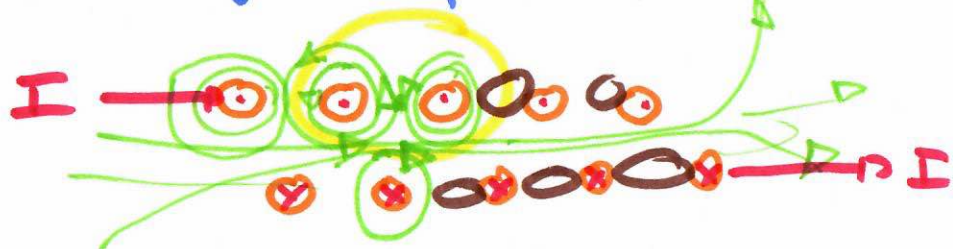
$$\oint_C \vec{H} \cdot d\vec{s} = I = \iint_A \vec{j} \cdot d\vec{A}$$

general law $\rightarrow$ One of Maxwell's Laws

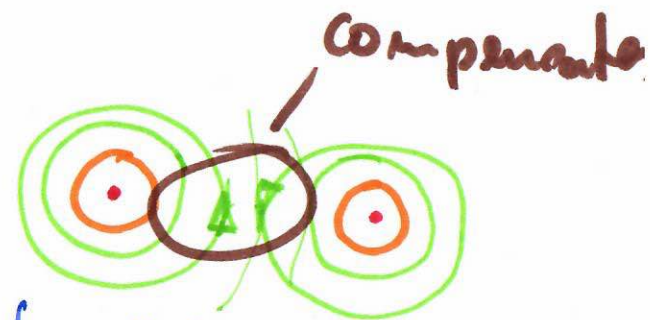
Also:



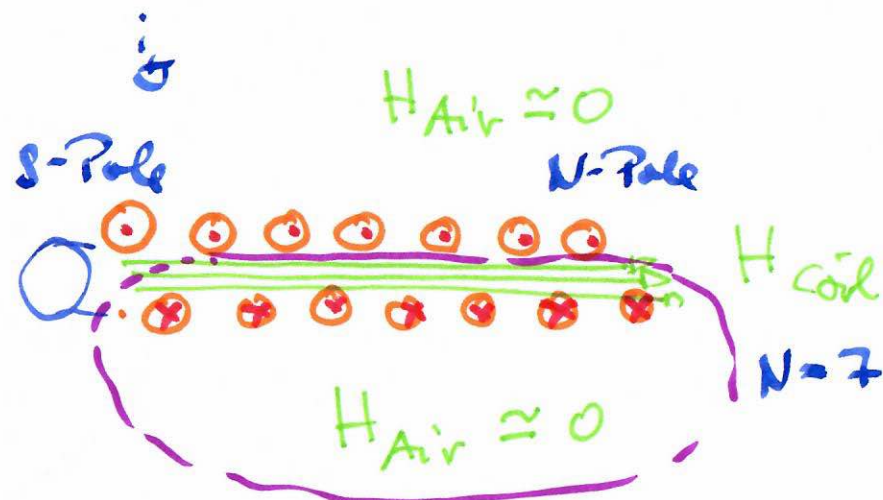
• The magnetic field of a coil ^{cyllinder}



③ ④



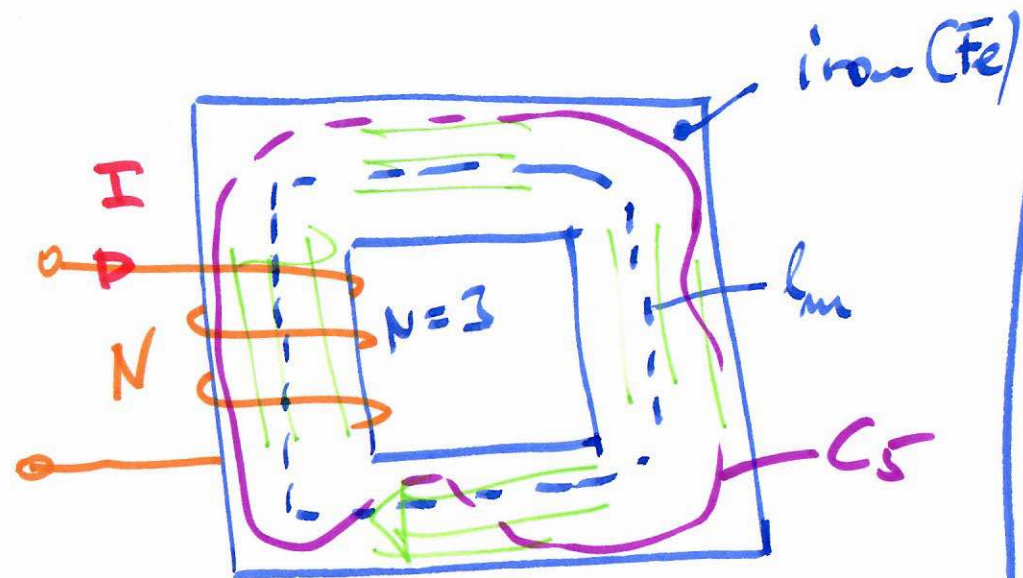
- copy fig. 4.4



$$\oint \vec{H} \cdot d\vec{s} = H_{\text{coil}} \cdot l = NI = 7I$$

$$H_{\text{coil}} = \frac{N I}{l} \quad \text{in } \frac{\text{A}}{\text{m}}$$

- Iron core with a coil



- magn. field lines like to go to iron and not to the air (as a current likes to go to metal conductor and not through plastic / wood conductors)

⑤

⑥

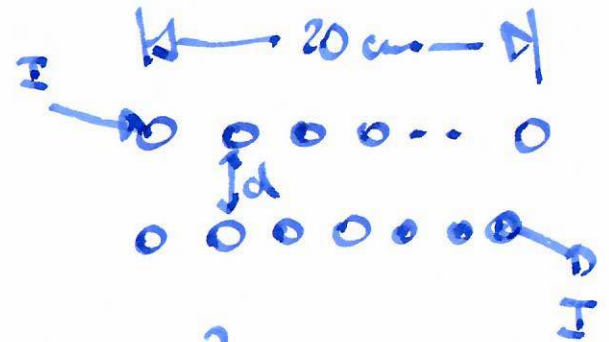
l_m : middle field strength length

$$\oint_{CS} \vec{H} \cdot d\vec{s} = NI \approx H \cdot l_m$$

$$H = H_{in.} = \frac{NI}{l_m} \quad \text{only by a "long" coil}$$

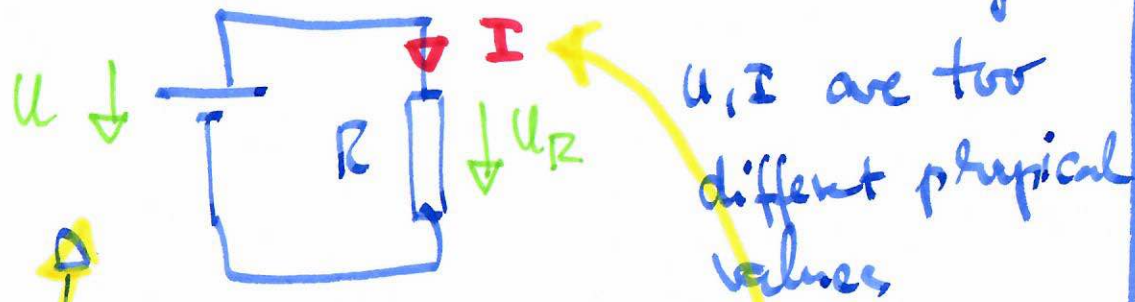
- Motor / drive of the magn. field is the current (I, NI)

Examples:

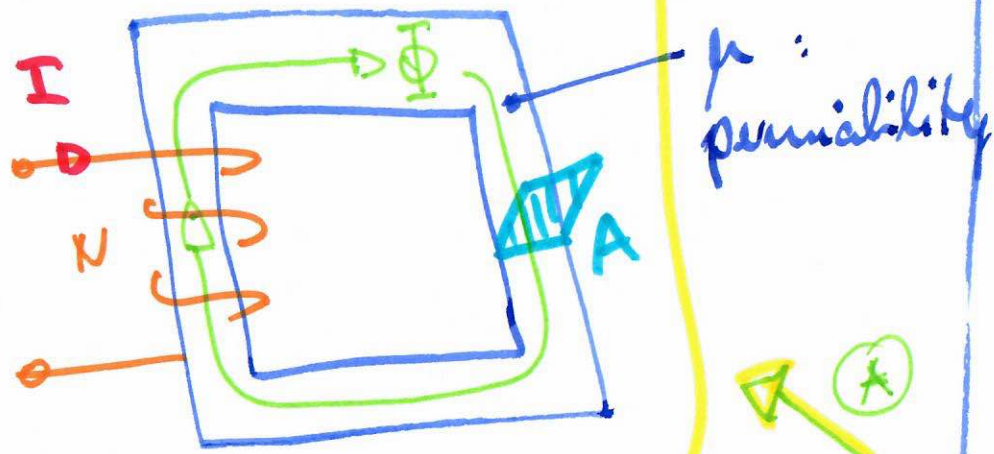


$$\left. \begin{array}{l} l = 20 \text{ cm} \\ I = 5 \text{ A} \\ d = 4 \text{ cm} (\ll 20 \text{ cm}) \\ N = 200 \end{array} \right\} H = \frac{200 \cdot 5 \text{ A}}{0.2 \text{ m}} = \underline{\underline{5000 \frac{\text{A}}{\text{m}}}}$$

- magnetic flux, magnetic flux density



in magnetic circuits we have also two different physical values



$N \cdot I$ and
magnetic voltage,
magnetic drive

and
magnetic flux

⑧

Permeability: "Number / magnetic conductivity"

$\mu = \mu_0 \cdot \mu_r$ relative permeability
↳ absolute permeability
 $= 4\pi \cdot 10^{-7} \frac{Vs}{Am}$

$\mu_r = 1$ in air, water, plastic, wood...

$\mu_r \gg 1$ in iron, ...

⇒ it is not usual to handle with flux, we handle with flux density

$$\vec{B} = \frac{\vec{\Phi}}{A} \quad \vec{\Phi} = \iint_A \vec{B} d\vec{A}$$

flux density, magn. induction

$$H \text{ in } \frac{A}{m}$$

$$\mu \text{ in } \frac{Vs}{Am}$$

$$\Phi \text{ in } Vs = Wb$$

$$I \text{ in } \frac{Vs}{m^2} = T$$

$$\sigma \text{ in } \frac{S}{m} \text{ Conduct.}$$

$$S \text{ in } \Omega \cdot m \text{ spec. resistance}$$

$$S = 1/\sigma$$

$$T = \frac{\rho g}{s^2 A} = \frac{N \cdot s^2 A}{m^2 \cdot s^2 A} = \frac{Vs}{m^2}$$

Seven base units

mol, ~~kg~~, A, s, m
deg, K, cd

$$1 \text{ Js} = 1 \text{ Nm} = 1 J$$

$$1 N =$$

$$\left(\begin{matrix} \vec{F} = m \vec{a} \\ \downarrow \quad \downarrow \quad \downarrow \\ N \quad kg \quad \frac{m}{s^2} \end{matrix} \right)$$

(10)

$$\text{Def } \vec{a} = \frac{d\vec{v}}{dt} ; \vec{v} = \frac{d\vec{s}}{dt}$$

↓ acceleration ↓ velocity, Speed

(W: work; P: Power, ...)

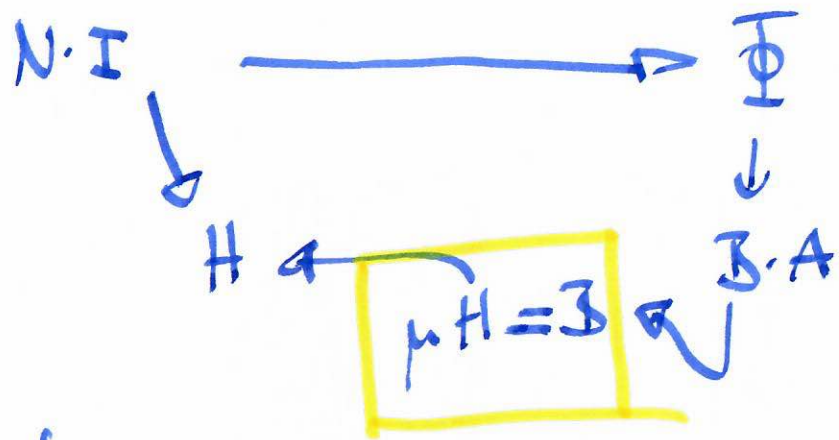
$$N = \rho g \cdot \frac{m}{s^2} ; \rho g = \frac{N \cdot s^2}{m}$$

$$N = \frac{Js}{m}$$

Examination question: show that $\frac{\rho g \cdot m^2}{s^2 A} = Vs$

$$\left(\begin{matrix} \vec{F} = m \vec{a} \\ \downarrow \quad \downarrow \quad \downarrow \\ N \quad kg \quad \frac{m}{s^2} \end{matrix} \right) \quad \sigma \text{ in } \frac{S}{m} \quad \boxed{E = mc^2}$$

see above: $\mathcal{B}$ (A)



$$\Rightarrow \Phi = B A = \mu \cdot H \cdot A$$

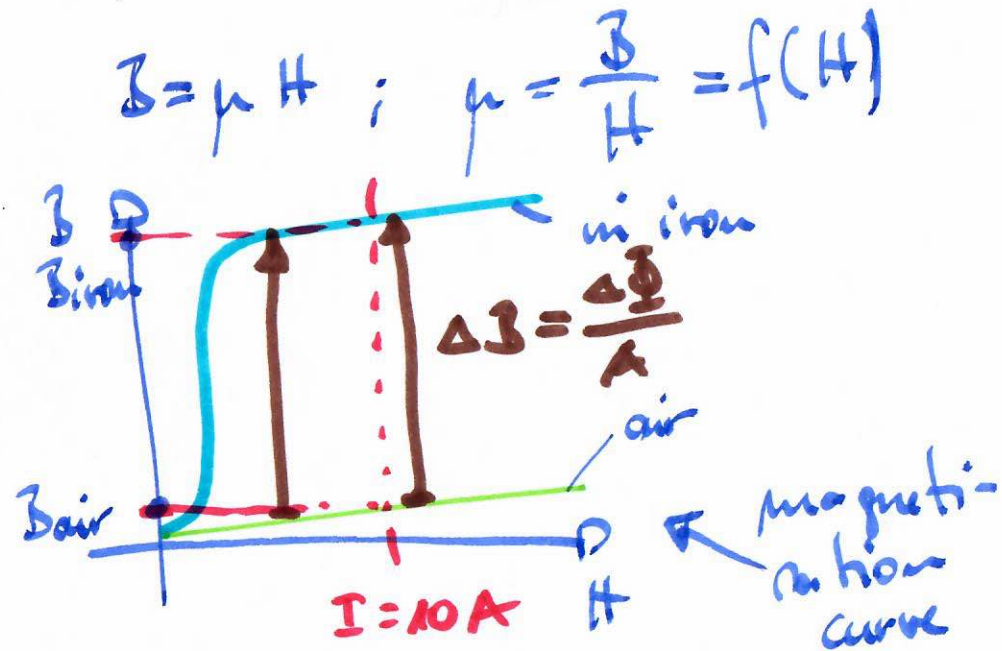
$$\Phi = \mu_0 \mu_r H \cdot A = \mu_0 \mu_r \cdot A \cdot \frac{IN}{l_m}$$

inside $\boxed{B = \mu_0 \mu_r H}$
 material
 constant as ϵ, μ

(11)

(12)

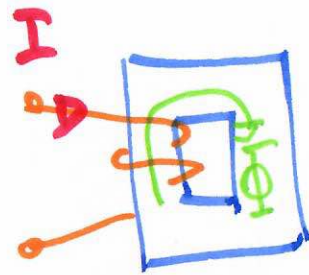
But $B = f(H) \rightarrow$ problem
 ↳ not linear



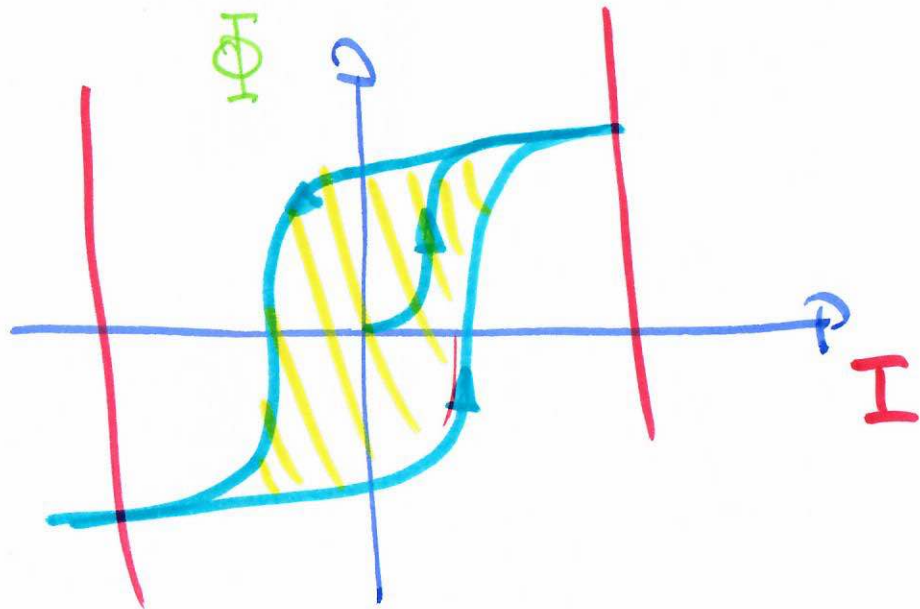
ΔB : Benefit of the iron.
 This is the reason why
 electric machines are always
 iron inside: motors, gener.,
 magnets, ...

• Hysteresis Curve / Loop

- same construction as at the top



(13)



Area of the curve:

$$\left[\int \Phi dI \right] = V_s \cdot A = W_s$$

↳ Work, Energy

(14)

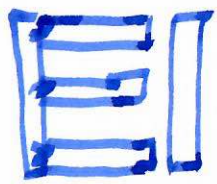
50 times / s this area =
energy is needed $\Rightarrow$

$$P_{L.H} \sim f \sim \text{loss Hysteresis}$$

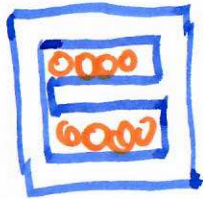
18.17.18, El. Machinery

• Iron Core with air gap

- See iron cores in the internet as:



E-I-core



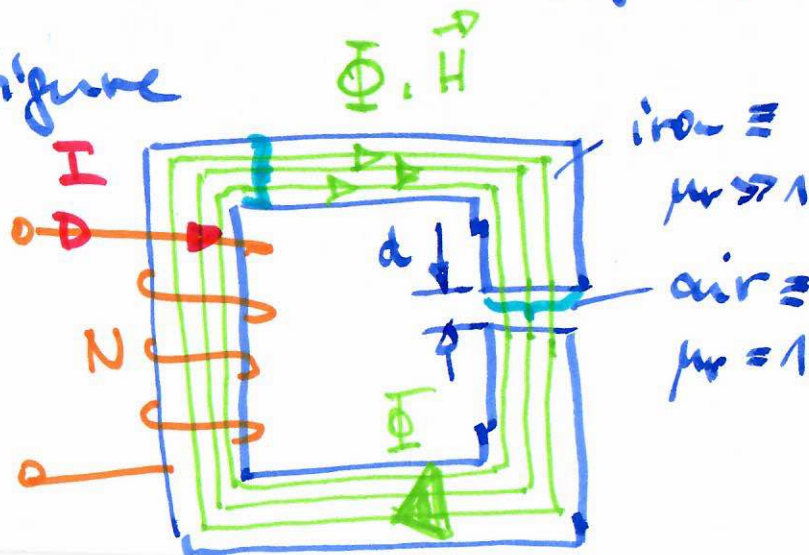
- no solid core, it

U-core consists of thin iron leaves

as in ET 22,

Fig 20a, 20b

- Figure



①

②

∇ all magnetic flux lines are closed ∇

} homogeneous

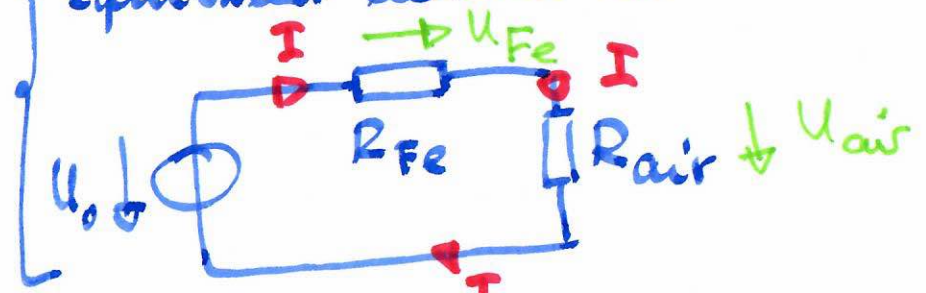
We run $\oint \vec{H} \cdot d\vec{s} = N \cdot I$

Area A is similar at all points of the core and in the air gap.

$\Phi = \text{const} = B \cdot A = \mu_0 \mu_r \cdot H \cdot A$

$l_{Fe}, l_{air} = d$

equivalent electric circuit:



$$\rightarrow H_{Fe} \cdot l_{Fe} + H_{air} \cdot d = N I \quad \textcircled{3}$$

$$\downarrow \begin{array}{l} B_{Fe} = B \\ \frac{B_{Fe}}{\mu_0 \mu_r} \left(B = \mu_0 \mu_r H \right) \end{array} \quad \frac{B_{air}}{\mu_0} = B$$

$$\underbrace{\Phi = \Phi_{air} = \Phi_{Fe}}_A = B = B_{air} = B_{Fe}$$

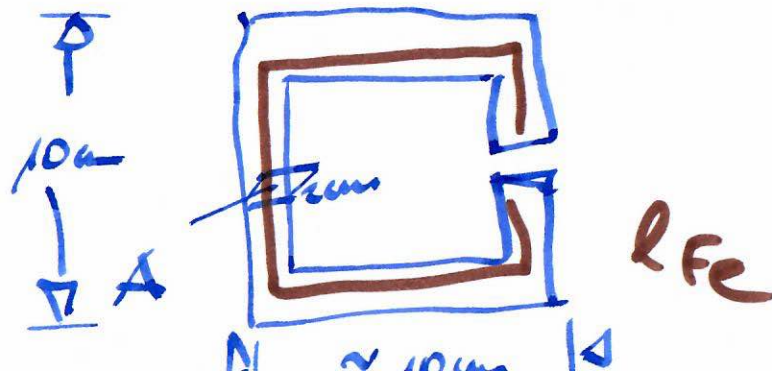
$$\frac{B}{\mu_0 \mu_r} \cdot l_{Fe} + \frac{B}{\mu_0} \cdot d = N \cdot I$$

$$B \left(\frac{l_{Fe}}{\cancel{\mu_0 \mu_r}} + \frac{d}{\cancel{\mu_0}} \right) = N \cdot I \mu_0$$

$$B = \frac{N I \mu_0}{\frac{l_{Fe}}{\mu_r} + d}$$

$$\Phi = \mu_0 \frac{N I A}{\frac{l_{Fe}}{\mu_r} + d}$$

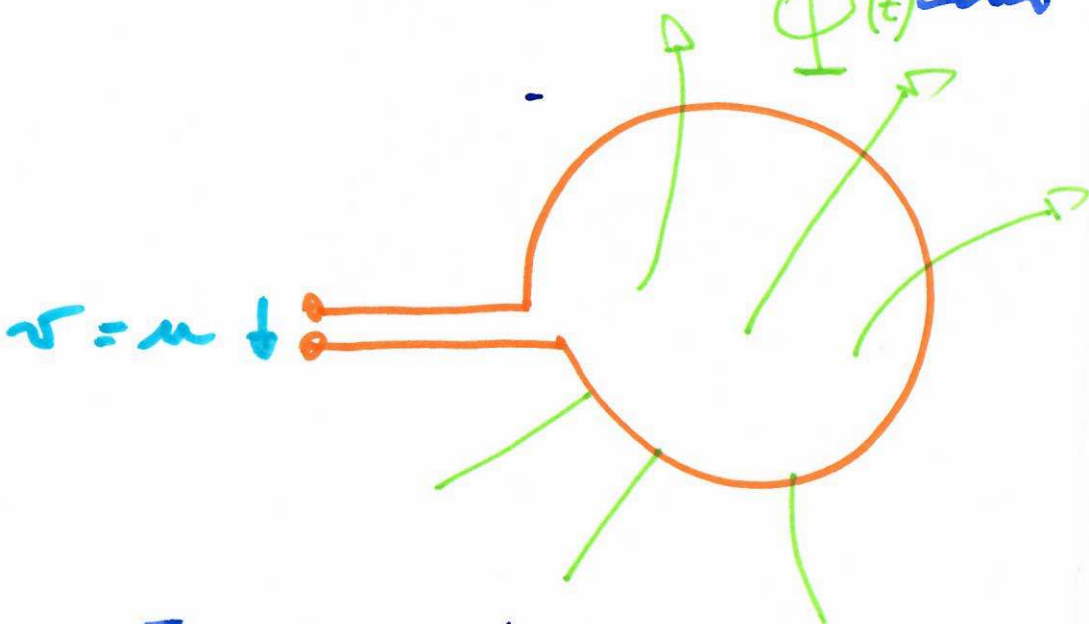
Example: $\mu_r = 200$; $l_{Fe} = 40 \text{ cm}$
 $d = 1 \text{ mm}$; $N = 500$
 $I = 5 \text{ A}$; $\mu_0 = 4\pi \cdot 10^{-7} \frac{\text{Vs}}{\text{Am}}$
 $A = 4 \text{ cm}^2$



⇒ the air gap needs a lot of "magnetic voltage" = NI
 So general the air gap should be small / short.

• Faraday's law / Induction

$\Phi(t)$ Law



Faraday observed: if the

⑥ magn. flux Φ is changing, a voltage v appears

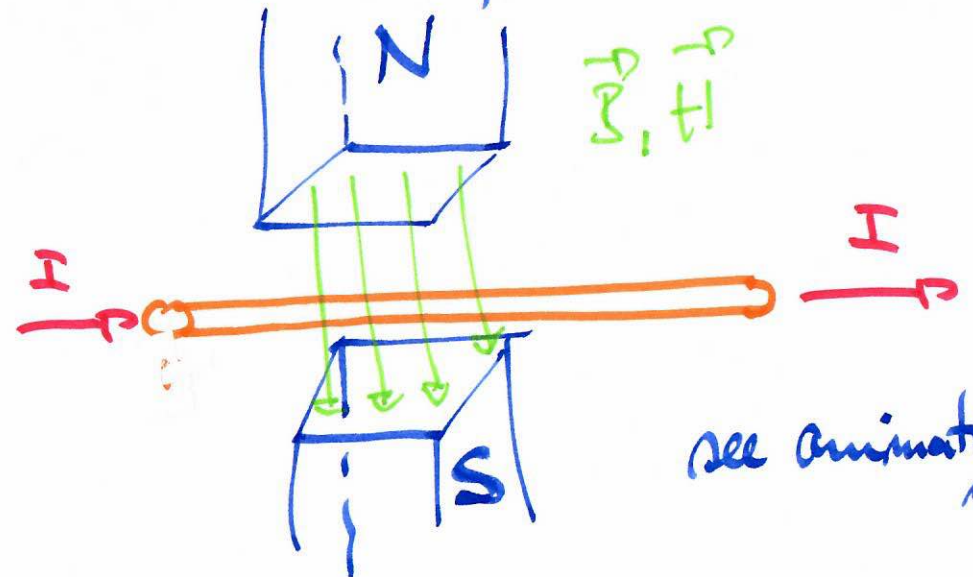
Induction Law

$$u = N \frac{d\Phi}{dt}$$

! im-
por-
tant

N : no. of windings

• Force on a wire in a magnetic field

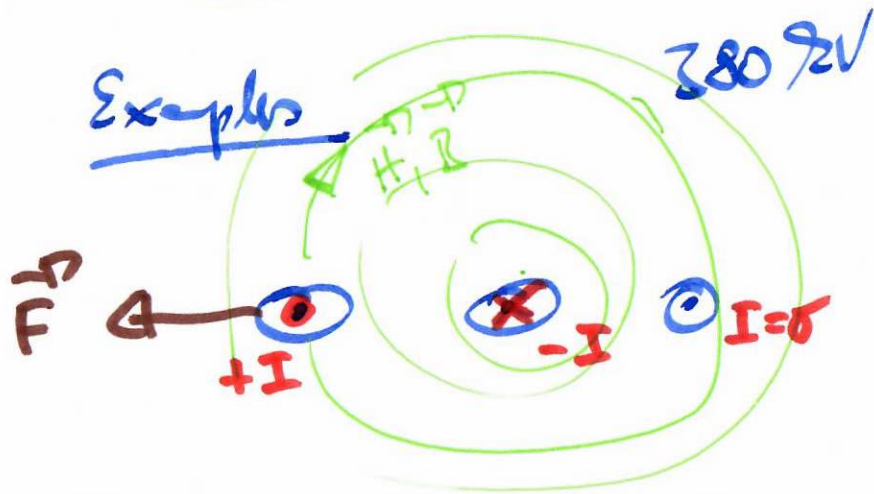


see animation

- direction of the force

⑦

rule: If the mag. field lines go into the inner of the open hand and the thumb shows to the direction of the current, then the other fingers show in to the direction of the force.



⑧

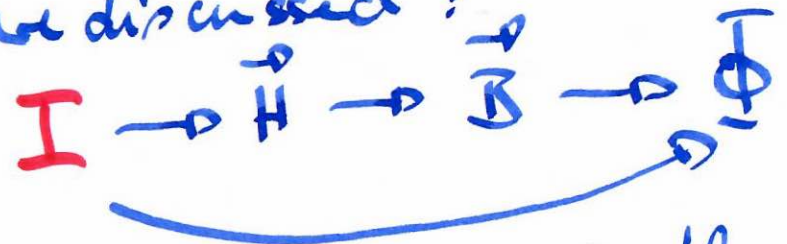
I: start circuit current
for ex. $10^4 \dots 10^6 \text{ A}$

• Lenz Rule

see: Skript ET14A or/and
Wikipedia

• Inductance, a parameter of a coil, characteristic of a coil

we discussed:



but to measure the flux
(in and out)

is not so simple! ⑨

People in history did calculate this. Magn. flux - what is it?

⚡ We need it in electr. circuit, ...
It can be found

$I \rightarrow \Phi$
 $I \sim \Phi$: (Costar $\sim$ mass)
 $\rightarrow$ proportionality

$$I = \alpha \Phi$$

only another form

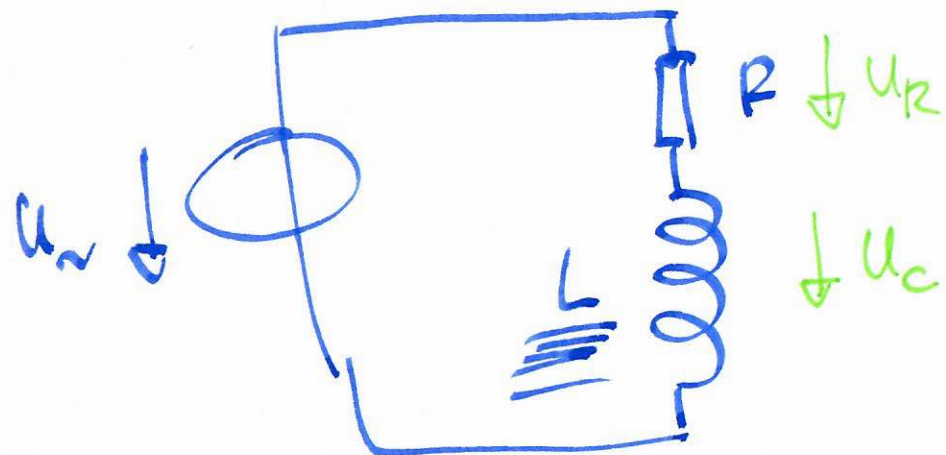
$$\Phi = L \cdot I \quad \text{or} \quad \boxed{L = \frac{\Phi}{I}} \quad \begin{array}{l} \text{Inductance} \\ \text{in} \\ H = \frac{Vs}{A} \end{array}$$

⑩

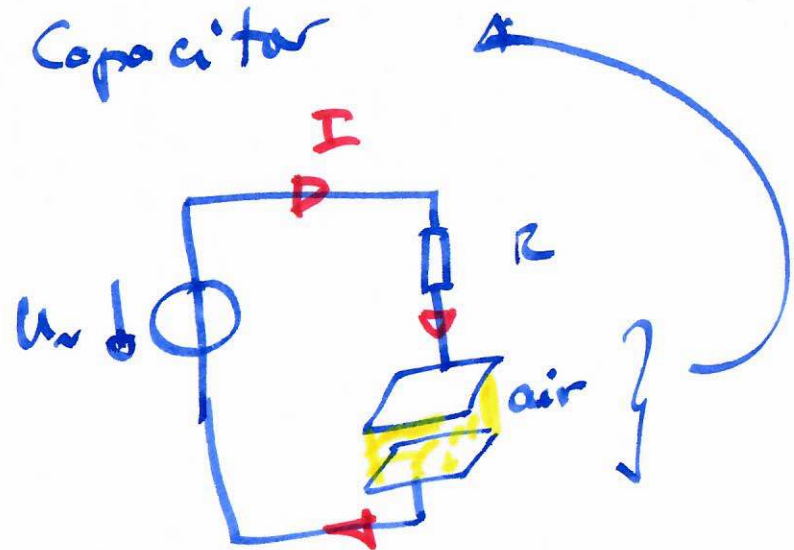


Inductances

Example:



• Capacitor



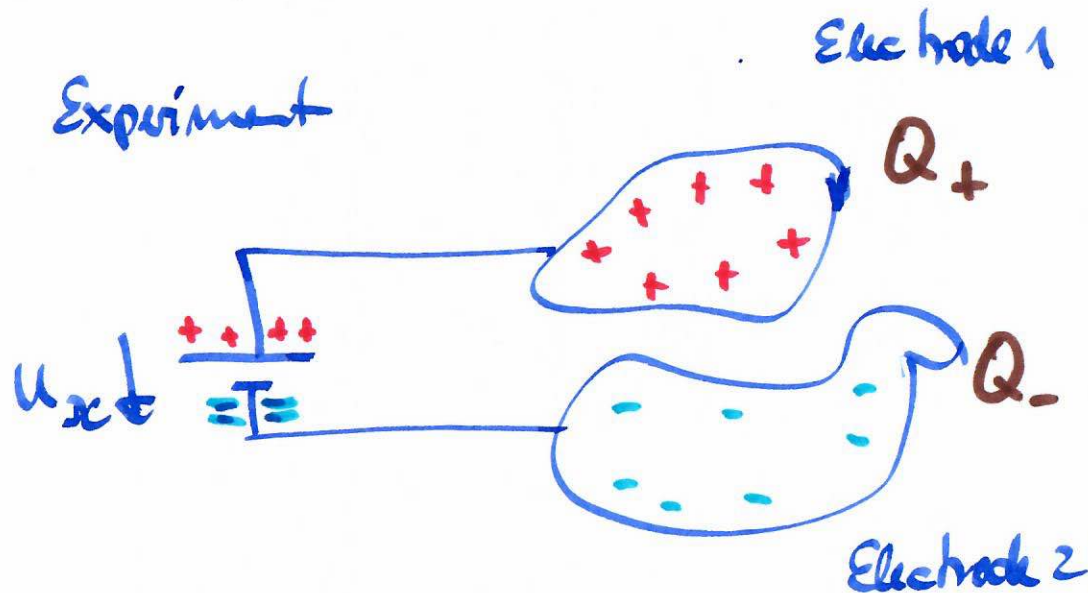
$$I = \frac{dQ}{dt}$$

1st reminder

(11)

Def. of current

Experiment



$$U_{DC} \rightarrow Q_+$$

$$\uparrow U_{DC} \rightarrow Q_+ \uparrow$$

$$\uparrow\uparrow U_{DC} \rightarrow Q_+ \uparrow\uparrow$$

(12)

$$U_{DC} = U \rightarrow Q_+ = Q$$

$$Q \sim U$$

$$Q = C \cdot U$$

$$C = \frac{Q}{U} \quad \text{in} \quad \frac{As}{V} = F \quad \text{Farad}$$

or

$$L = \frac{\Phi}{I} \quad \text{in} \quad \frac{Vs}{A} = H$$

Henry

it follows

$$u = L \frac{di}{dt}$$

$$i = C \frac{du}{dt}$$